

Q12 * Mathematik m3 * Berechnung einfacher bestimmter Integrale

$$\int_{-1}^2 (3x-1) dx = \left[\frac{3x^2}{2} - x \right]_{-1}^2 = \left(\frac{3 \cdot 4}{2} - 2 \right) - \left(\frac{3}{2} - (-1) \right) = 4 - 2,5 = 1,5$$

$$\int_0^2 2\sqrt{x} + 0,5x dx = \int_0^2 2 \cdot x^{1/2} + 0,5x dx = \left[\frac{2 \cdot x^{3/2}}{3/2} + \frac{0,5x^2}{2} \right]_0^2 = \left[\frac{4}{3} x\sqrt{x} + \frac{1}{4} x^2 \right]_0^2 = \frac{8}{3} \sqrt{2} + \frac{1}{4} \cdot 4 - 0 = 1 + \frac{8}{3} \sqrt{2}$$

$$\int_1^3 \frac{2}{\sqrt{x}} dx = \int_1^3 2 \cdot x^{-1/2} dx = \left[2 \cdot \frac{x^{1/2}}{1/2} \right]_1^3 = \left[4\sqrt{x} \right]_1^3 = 4\sqrt{3} - 4 (= 4 \cdot (\sqrt{3} - 1))$$

$$\int_0^1 (x+2)^2 dx = \int_0^1 x^2 + 4x + 4 dx = \left[\frac{x^3}{3} + \frac{4x^2}{2} + 4x \right]_0^1 = \frac{1}{3} + 2 + 4 - 0 = \frac{19}{3} \quad \text{oder}$$

$$= \left[\frac{(x+2)^3}{3} \right]_0^1 = \frac{3^3}{3} - \frac{2^3}{3} = \frac{27-8}{3} = \frac{19}{3}$$

$$\int_{-1}^1 (2x-1)^2 dx = \left[\frac{(2x-1)^3}{3 \cdot 2} \right]_{-1}^1 = \frac{1}{6} - \frac{(-3)^3}{6} = \frac{28}{6} = \frac{14}{3}$$

oder

$$\int_{-1}^1 4x^2 - 4x + 1 dx = \left[\frac{4x^3}{3} - \frac{4x^2}{2} + x \right]_{-1}^1 = \frac{4}{3} - 2 + 1 - \left(-\frac{4}{3} - 2 - 1 \right) = \frac{8}{3} + 2 = \frac{14}{3}$$

$$\int_{-1}^1 (2-x)^4 dx = \left[\frac{(2-x)^5}{-5} \right]_{-1}^1 = \frac{1}{-5} - \left(\frac{3^5}{-5} \right) = \frac{243}{5} - \frac{1}{5} = \frac{242}{5}$$

$$\int_{-2}^2 x^5 - 4x^3 + 2x dx = 0, \text{ da } f(x) \text{ einen zum Ursprung punktsymmetr. Graphen besitzt.}$$

$$\int_0^2 3 \cdot \sqrt{2x+1} dx = \left[\frac{3 \cdot (2x+1)^{3/2}}{2 \cdot \frac{3}{2}} \right]_0^2 = \left[(2x+1)^{3/2} \right]_0^2 = 5\sqrt{5} - 1$$